Math 253 – Fall 2008 Test 1 (Version 2) Name:_ You must show appropriate work for credit.

- 1) Find the equation of the plane that intersects the *xz*-plane along the line z = 10 2x and intersects the *yz*-plane along the line z = 10 5y
- 2) Express $f(x, y) = \sin(5x^2 3y)$ as one particular level surface of a function g(x, y, z) (there are many possible answers).

The g = _____ level surface of g(x, y, z) = _____

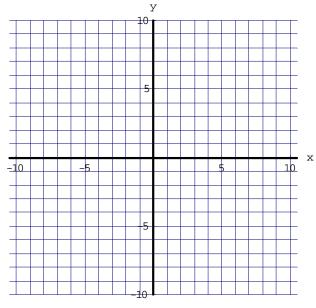
3) v = 4i + 4j + 2k, w = 2i + 3j + 6k

- a) $\mathbf{v} \cdot \mathbf{w} =$
- b) $\mathbf{v} \times \mathbf{w} =$
- c) What is the angle (in radians) formed by **v** and **w**?
- d) What is the equation of the plane containing **v**, **w** and the point (1, -2, -5)? (note: you do not need to solve the equation for *z*)
- 4) For each function, calculate the following derivatives: f_x , f_y

a)
$$f(x, y) = 5x^2 + 3x^2y - 4y^3$$

b)
$$f(x, y) = e^{y^2 - 4x}$$

- 5) z = f(x, y) = xy
 - a.) Make a contour diagram of *f* for the following *z*-values: z = -4, -1, 1, 4. Be sure to label your level <u>curves</u>.



b.) Draw a 3D sketch of the graph of *f*, and briefly describe the graph in words.